

$$10) \quad 3[g(x)]^2 \cdot g'(x)$$

$$3 \cdot (-3)^2 \cdot 6$$

KEY

K	Find the rate of change of $y = (4x^3 + 7x^2 + 1)^2$ at $x = -1$.	-16	✓
N	$f(x) = \sqrt{x^2 + 2x + 8}$ find the instantaneous rate of change at 2	$\frac{3}{4}$	✓
O	$f(x) = \frac{3x+2}{x-1}$ find $f'(0)$	-5	✓
W	$f(x) = \frac{1}{3}x\sqrt{x^2 + 5}$ find $f'(2)$	13/9	✓
L	Find the average rate of change of $g(x) = x^2 + e^x$ $[0, 1]$	E	✓
I	A particle's motion is modeled by the function $x(t) = x^2 - 4x - 3$. Find the average velocity on the interval $[0, 3]$	-1	✓
M	Find where the function $\ln(x^2 - 3x + 5)$ has a horizontal tangent	3/2	✓
I	$s(t) = 3t^4 - 8t^3 + 6t^2 + 3$. When does the particle change directions on the interval $[-10, 10]$	0	✓
T	$f(x) = \frac{1}{9}(3x+1)^3$ find $f''(1)$	24	✓
S	$G(5) = -3, g'(5) = 6, h(5) = 3$ and $h'(5) = -2$, find $f'(5)$ if $f(x) = [g(x)]^3$	162	✓

$$f'(x) =$$

$$1) \quad 2(4x^3 + 7x^2 + 1)' \cdot (12x^2 + 14x)$$

$$2(-4 + 7 + 1) \cdot (12 - 14)$$

$$2(4) \cdot -2$$

$$8 \cdot -2 = -16$$

$$4) \quad \frac{1}{3}x \cdot (x^2 + 5)^{1/2}$$

$$f'(x) = \frac{1}{3}x \left[\frac{1}{2}(x^2 + 5)^{-1/2} \cdot 2x \right]$$

$$+ (x^2 + 5)^{1/2} \cdot \frac{1}{3}$$

$$\frac{2}{3} \left[\frac{1}{6} \cdot 4 \right]$$

$$+ 3 \cdot \frac{1}{3}$$

$$2) \quad f(x) = (x^2 + 2x + 8)^{1/2}$$

$$f'(x) = \frac{1}{2}(x^2 + 2x + 8)^{-1/2} \cdot (2x + 2)$$

$$\frac{1}{2}(4 + 4 + 8)^{-1/2} \cdot (6)$$

$$\frac{1}{2\sqrt{16}} \cdot 6 = \frac{6}{8} = \frac{3}{4}$$

$$\frac{2}{3} \left(\frac{2}{3} \right) + 1$$

$$\frac{4}{9} + 1$$

$$\frac{13}{9}$$

$$3) \quad f'(x) = \frac{(x-1)(3) - (3x+2)(1)}{(x-1)^2} = \frac{3x-3-3x-2}{(x-1)^2}$$

$$\frac{0-3-0-2}{1} = -5$$

$$5) \frac{g(1) - g(0)}{1 - 0} \quad g(x) = x^2 + e^x$$

$$\frac{1 + e - 1}{1} = \frac{e}{1} = e$$

$$6) \frac{x(3) - x(0)}{3 - 0} = \frac{-6 - (-3)}{3} = -1$$

$$7) \frac{1}{x^2 - 3x + 5} \cdot 2x - 3$$

$$2x - 3 = 0$$

$$x = \frac{3}{2}$$

$$8) s(t) = 3x^4 - 8x^3 + 6x^2 + 3$$

$$v(t) = 12x^3 - 24x^2 + 12x = 0$$

$$12x(x^2 - 2x + 1) = 0$$

$$12x(x-1)(x-1) = 0$$

$$x = 0, 1$$



$$9) f(x) = \frac{1}{9}(3x+1)^3$$

$$f'(x) = \frac{1}{3}(3x+1)^2 \cdot 3$$

$$f''(x) = 2(3x+1) \cdot 3 = 6(3x+1)$$

$$f''(1) = 6(3+1) = 24$$