

2007 AB5/BC5:

(c)  $\int_0^{12} r'(t) dt \approx 2(4.0) + 3(2.0) + 2(1.2) + 4(0.6) + 1(0.5)$   
 $= 19.3$  ft

$\int_0^{12} r'(t) dt$  is the change in the radius, in feet, from  
 $t = 0$  to  $t = 12$  minutes.

(d) Since  $r$  is concave down,  $r'$  is decreasing on  $0 < t < 12$ .  
Therefore, this approximation, 19.3 ft, is less than

$$\int_0^{12} r'(t) dt.$$

Units of  $\text{ft}^3/\text{min}$  in part (b) and ft in part (c)

2 :  $\left\{ \begin{array}{l} 1 : \text{approximation} \\ 1 : \text{explanation} \end{array} \right.$

1 : conclusion with reason

1 : units in (b) and (c)

2004 AB3/BC3 (Form B):

(a) Midpoint Riemann sum is  
 $10 \cdot [v(5) + v(15) + v(25) + v(35)]$   
 $= 10 \cdot [9.2 + 7.0 + 2.4 + 4.3] = 229$

The integral gives the total distance in miles that the  
plane flies during the 40 minutes.

3 :  $\left\{ \begin{array}{l} 1 : v(5) + v(15) + v(25) + v(35) \\ 1 : \text{answer} \\ 1 : \text{meaning with units} \end{array} \right.$

2002 AB4/BC4 (Form B):

$$(d) \frac{3}{2}(-1 + 2(0 + 1 + 3 + 1 + 0) - 1) \\ = 12$$

1 : trapezoidal method

2001 AB2/BC2:

$$(b) \frac{3}{2}(20 + 2(31) + 2(28) + 2(24) + 2(22) + 21) = 376.5 \\ \text{Average temperature} \approx \frac{1}{15}(376.5) = 25.1^\circ\text{C}$$

2 :  $\begin{cases} 1 : \text{trapezoidal method} \\ 1 : \text{answer} \end{cases}$