

Review for Differential Equations

The graph of  $y = 5x^4 - x^5$  has a point of inflection at

- (A) (0,0) only                      (B) (3,162) only                      (C) (4,256) only  
(D) (0,0) and (3,162)              (E) (0,0) and (4,256)

The area of the region bounded by the lines  $x = 0$ ,  $x = 2$ , and  $y = 0$  and the curve  $y = e^{\frac{x}{2}}$  is

- (A)  $\frac{e-1}{2}$               (B)  $e-1$               (C)  $2(e-1)$               (D)  $2e-1$               (E)  $2e$

The region enclosed by the graph of  $y = x^2$ , the line  $x = 2$ , and the  $x$ -axis is revolved about the  $y$ -axis. The volume of the solid generated is

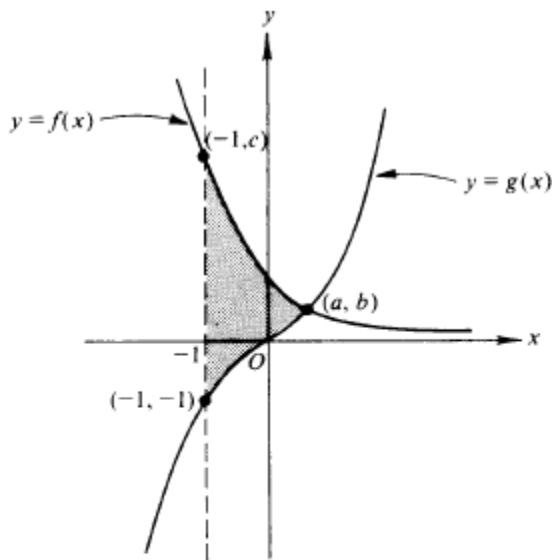
- (A)  $8\pi$               (B)  $\frac{32}{5}\pi$               (C)  $\frac{16}{3}\pi$               (D)  $4\pi$               (E)  $\frac{8}{3}\pi$

Solve the differential equation  $e^{x+y} dy = dx$ .

- a)  $e^{-x} + e^y = C$                       b)  $e^{-x} + e^{-y} = C$                       c)  $e^x + e^y = C$   
d)  $e^x + e^{-y} = C$                       e)  $e^{-x} + 2e^{-y} = C$

The base of a solid is a circular region in the  $xy$ -plane bounded by the graph of  $x^2 + y^2 = 36$ . Find the volume of the solid if every cross section by a plane normal to the  $x$ -axis is an equilateral triangle with one side on the base.

- a)  $72\sqrt{3}$               b)  $288\sqrt{3}\pi$               c)  $144\sqrt{3}\pi$               d)  $144\sqrt{3}$               e)  $288\sqrt{3}$



The curves  $y = f(x)$  and  $y = g(x)$  shown in the figure above intersect at the point  $(a, b)$ . The area of the shaded region enclosed by these curves and the line  $x = -1$  is given by

- (A)  $\int_0^a (f(x) - g(x)) dx + \int_{-1}^0 (f(x) + g(x)) dx$
- (B)  $\int_{-1}^b g(x) dx + \int_b^c f(x) dx$
- (C)  $\int_{-1}^c (f(x) - g(x)) dx$
- (D)  $\int_{-1}^a (f(x) - g(x)) dx$
- (E)  $\int_{-1}^a (|f(x)| - |g(x)|) dx$

Which of the following gives the area of the surface generated by revolving about the  $y$ -axis the arc of  $x = y^3$  from  $y = 0$  to  $y = 1$ ?

- (A)  $2\pi \int_0^1 y^3 \sqrt{1+9y^4} dy$
- (B)  $2\pi \int_0^1 y^3 \sqrt{1+y^6} dy$
- (C)  $2\pi \int_0^1 y^3 \sqrt{1+3y^2} dy$
- (D)  $2\pi \int_0^1 y \sqrt{1+9y^4} dy$
- (E)  $2\pi \int_0^1 y \sqrt{1+y^6} dy$

The region in the first quadrant between the  $x$ -axis and the graph of  $y = 6x - x^2$  is rotated around the  $y$ -axis. The volume of the resulting solid of revolution is given by

- (A)  $\int_0^6 \pi(6x - x^2)^2 dx$   
(B)  $\int_0^6 2\pi x(6x - x^2) dx$   
(C)  $\int_0^6 \pi x(6x - x^2)^2 dx$   
(D)  $\int_0^6 \pi(3 + \sqrt{9 - y})^2 dy$   
(E)  $\int_0^9 \pi(3 + \sqrt{9 - y})^2 dy$

The base of a solid is the region enclosed by the graph of  $y = e^{-x}$ , the coordinate axes, and the line  $x = 3$ . If all plane cross sections perpendicular to the  $x$ -axis are squares, then its volume is

- (A)  $\frac{(1 - e^{-6})}{2}$     (B)  $\frac{1}{2}e^{-6}$     (C)  $e^{-6}$     (D)  $e^{-3}$     (E)  $1 - e^{-3}$

A region in the first quadrant is enclosed by the graphs of  $y = e^{2x}$ ,  $x = 1$ , and the coordinate axes. If the region is rotated about the  $y$ -axis, the volume of the solid that is generated is represented by which of the following integrals?

- (A)  $2\pi \int_0^1 x e^{2x} dx$   
(B)  $2\pi \int_0^1 e^{2x} dx$   
(C)  $\pi \int_0^1 e^{4x} dx$   
(D)  $\pi \int_0^e y \ln y dy$   
(E)  $\frac{\pi}{4} \int_0^e \ln^2 y dy$

An equation of the line tangent to the graph of  $y = \frac{2x+3}{3x-2}$  at the point  $(1, 5)$  is

- (A)  $13x - y = 8$     (B)  $13x + y = 18$     (C)  $x - 13y = 64$   
(D)  $x + 13y = 66$     (E)  $-2x + 3y = 13$

If the region enclosed by the  $y$ -axis, the line  $y = 2$ , and the curve  $y = \sqrt{x}$  is revolved about the  $y$ -axis, the volume of the solid generated is

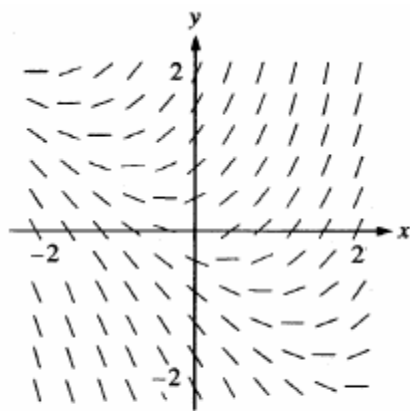
- (A)  $\frac{32\pi}{5}$       (B)  $\frac{16\pi}{3}$       (C)  $\frac{16\pi}{5}$       (D)  $\frac{8\pi}{3}$       (E)  $\pi$

An equation of the line tangent to the graph of  $y = x + \cos x$  at the point  $(0, 1)$  is

- (A)  $y = 2x + 1$       (B)  $y = x + 1$       (C)  $y = x$       (D)  $y = x - 1$       (E)  $y = 0$

What is the area of the region between the graphs of  $y = x^2$  and  $y = -x$  from  $x = 0$  to  $x = 2$ ?

- (A)  $\frac{2}{3}$       (B)  $\frac{8}{3}$       (C) 4      (D)  $\frac{14}{3}$       (E)  $\frac{16}{3}$



Shown above is a slope field for which of the following differential equations?

- (A)  $\frac{dy}{dx} = 1 + x$       (B)  $\frac{dy}{dx} = x^2$       (C)  $\frac{dy}{dx} = x + y$       (D)  $\frac{dy}{dx} = \frac{x}{y}$       (E)  $\frac{dy}{dx} = \ln y$

The area enclosed by the curves  $y = x^2 - 4$  and  $y = 2x - 4$  can be represented by the integral

- (A)  $\int_{-4}^0 (x^2 - 2x) dx$   
 (B)  $\int_0^2 (2x - x^2) dx$   
 (C)  $\int_{-4}^0 (2x - x^2) dx$   
 (D)  $\int_0^2 (x^2 - 2x) dx$   
 (E)  $\int_{-4}^2 (x^2 - 2x) dx$