AP Calculus

3.4 Worksheet

All work must be shown in this course for full credit. Unsupported answers may receive NO credit.

1. What is the relationship between position, velocity, and acceleration?

P(x) = position P'(x) = velocity P'(x) = accel.

2. Once again trying to blow up earth because it interferes with his view of Venus, Marvin the Martian lands on the moon. Bugs Bunny, as always, interferes with his plan. Chasing Bugs, Marvin fires a warning shot straight up into the air with his Acme Disintegration Pistol. The height (in feet) after t seconds of the shot is given by



- $s(t) = -2.66t^2 + 135t + 3$.
- a) Find the velocity and acceleration as functions of time. (What is the meaning of the acceleration function?)

a(t) = -5.32 — Constant accel Jue b) What is the position of the shot when the velocity is 0? to gravity an Moun. V(t) = -5.32t + 135 = 0 t = 25.375...

$$V(t) = -5.32t + 135 = 0 t$$

5(25.37.) = 1715.876 A

3. Fill in the blanks.

a) When the <u>velocity</u> is positive, the object is moving in a positive direction.

b) An object is Sluwing down when the velocity and acceleration have different signs.

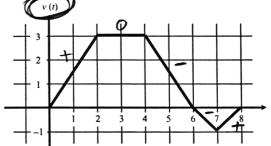
c) An object is stopped when ______ is zero.

d) Speed is always positive because it is the __abs. value

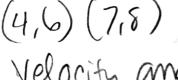
4. A bug begins to crawl up a vertical wire at time t = 0. The velocity, v, of the bug at time t, $0 \le t \le 8$ is given by the function whose graph is shown below.

a) At what value of t does the bug change direction?

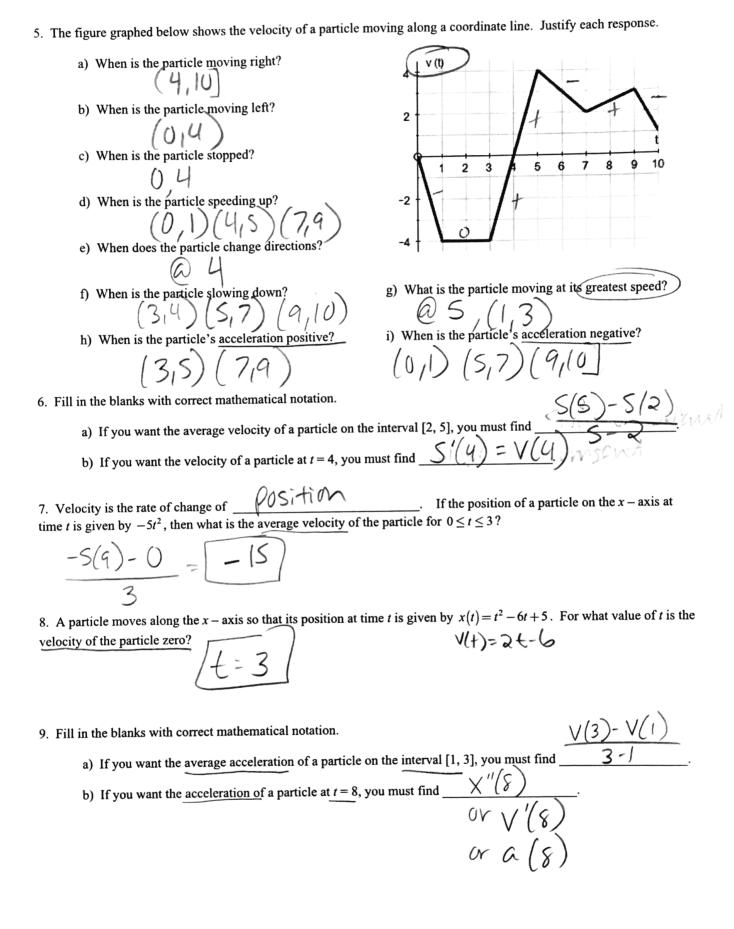




b) During which time intervals in the bug slowing down? Justify your response.







10. Rocket A has a positive velocity v(t) after being launched upward from an initial height of 0 feet at time t = 0seconds. The velocity of the rocket is recorded for selected values of t over the interval $0 \le t \le 80$ seconds as shown in the table below.

t (sec)	0	10	20	30	40	50	60	70	80
v (t) (ft/sec)	5	14	22	29	35	40	44	47	49
9 0 7 1 0 0 0									

a) Find the average acceleration of Rocket A over the time interval $0 \le t \le 80$ seconds. Indicate units of measure.

$$\frac{49-5}{80} = \frac{44}{80} + \frac{11}{80} = \frac{11}{20} + \frac{11}{80}$$

b) Using the data in the table, find an estimate for v'(35). Indicate units of measure.

$$\frac{\sqrt{(35)}}{\sqrt{(35)}} = \frac{\sqrt{(40)} - \sqrt{(30)}}{\sqrt{(0-30)}} = \frac{35 - 29}{46-30} = 0.6$$

- 11. A particle moves along the x-axis so that its position at any time $t \ge 0$ is given by the function $x(t) = t^3 12t + 1$, where x is measured in feet and t is measured in seconds. Justify each response and indicate units of measure when appropriate.
 - a) Find the displacement during the first 3 seconds.

$$X(0) = 1$$

 $X(3) = 27 - 36 + 1 = -8$ 9 A

c) Find the instantaneous velocity at t = 3 seconds.

e) When is the particle moving left?

when is the particle moving lett?
$$\sqrt{(+)} = 3(3-10) = 3(3+12)(3-12)$$

g) When is the particle speeding up?
$$(2, \infty)$$

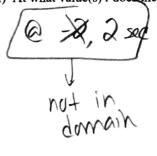
b) Find the average velocity during the first 3 seconds.

$$\frac{x(3)-x(0)}{3}=\frac{-8-1}{3}=\frac{-9}{3}=\frac{-3}{5}$$

d) Find the acceleration when t = 3 seconds.

$$a(t) = 6t$$
 $a(3) = [18 ft/sec^{3}]$

f) At what value(s) t does the particle change direction?



13. [Calculator] The cost involved in maintaining annual inventory for a certain manufacturer is given by $C(x) = \frac{1,008,000}{1} + 6.3x$, where x is the number of items stored. Find the marginal cost of storing the 351st item.

