

1. a) units -  $\frac{ft}{total}$   
Indicates distance traveled

b) Intervals:  $(10, 30)$ ,  $(30, 50)$ ,  $(50, 70)$

Midpoint	$x$	$y$
	20	22
	40	35
	60	44
	<hr/>	
	101	

$$M(3) = (101) \underset{\substack{\uparrow \\ \text{width}}}{20} = 2020$$

$$2. a) T'(7) = \frac{55 - 62}{8 - 6} = -\frac{7}{2} \text{ } ^\circ\text{C}/\text{min}$$

$$b) \frac{1}{8} \int_0^8 T(x) dx$$

$$T(n) = \frac{1}{2} (100 + 93) 1$$

$$+ \frac{1}{2} (93 + 70) 4$$

$$+ \frac{1}{2} (70 + 62) 1$$

$$+ \frac{1}{2} (62 + 55) 2$$

$$= 605.5$$

$$\frac{1}{8} (605.5) = 75.69$$

Because the subintervals  
are not equal, we have  
to find the area of each  
Trapezoid

3. (0.1, 0.2) (0.2, 0.3) (0.3, 0.4) (0.4, 0.5)  
 (0.5, 0.6) (0.6, 0.7) (0.7, 0.8) (0.8, 0.9) (0.9, 1.0)

$$\frac{0.1}{2} \left( 22 + 2(28) + 2(32) + 2(34) + 2(34) + \right. \\ \left. 2(32) + 2(28) + 2(22) + \right. \\ \left. 2(14) + 4 \right)$$

237 units<sup>2</sup>

4.  $\frac{1}{2} [ 0 + 2(50) + 2(60) + 2(80) + 2(90) + \dots$   
 $+ 2(100) + 2(95) + 2(85) + 2(80)$   
 $+ 2(75) + 85 ]$

$\frac{1}{2} [1515] \text{ mph} \cdot \text{min}$

$\frac{757.5}{60} = 29.29 \text{ miles}$

60 ← convert to minutes

5.  $\int_{-2}^2 4 - x^2$   
 LRAM

- f(-2) = 0
- f(-1) = 3
- f(0) = 4
- f(1) = 3

(10) |  
 13 units<sup>2</sup>

- MRAM
- f(-1.5) = 1.75
  - f(-0.5) = 3.75
  - f(0.5) = 3.75
  - f(1.5) = 1.75

(11) |  
 11 units<sup>2</sup>

- RRAM
- f(-1) = 3
  - f(0) = 4
  - f(1) = 3
  - f(2) = 0

(10) |  
 10 units<sup>2</sup>

5.  
TRAM

$$\frac{1}{2} [0 + 2(3) + 2(4) + 2(3) + 0]$$

$$\frac{1}{2} [4 + 8 + 6]$$
$$\frac{1}{2} (20)$$
$$10$$

6. a) LRAM

$$f(0) = 0$$

$$f(1) = 6$$

$$f(2) = 10$$

$$f(3) = 16$$

$$f(4) = 14$$

$$f(5) = 12$$

$$f(6) = 18$$

$$f(7) = 22$$

$$f(8) = 12$$

$$f(9) = 4$$

$$(116)1$$

116 inches

b) RRAM

$$f(1) = 6$$

$$f(2) = 10$$

$$f(3) = 16$$

$$f(4) = 14$$

$$f(5) = 12$$

$$f(6) = 18$$

$$f(7) = 22$$

$$f(8) = 12$$

$$f(9) = 4$$

$$f(10) = 2$$

$$(118)1$$

118 inches

$$7. (4,3)(1,2) + (3,1)(1,1) + (2,2)(1,5) + (1,5)(1,6)$$
$$14,22$$
$$B$$

$$8. \frac{1}{8} [24 + 76 + 106 + 124 + 135] 5$$

93°C

$$9. \frac{1}{2} [0 + 2(6) + 2(10) + 2(16) + 2(14) + 2(12) + 2(18) + 2(22) + 2(12) + 2(4) + 2]$$

$$= 115 \text{ inches}$$

$$10. \frac{1}{2} [4 + 2(1) + 2(0) + 2(1) + 4]$$

$$= 6$$

$$11. \frac{1}{2} [10 + 20] \approx \frac{1}{2} [20 + 40] + \frac{1}{2} [40 + 20]$$

D

$$12. a) R'(45) = \frac{55 - 40}{50 - 40} = \frac{15}{10} = 1.5 \frac{\text{gallons}}{\text{min}^2}$$

$$b) (0, 30) (30, 40), (40, 50) (50, 70) (70, 90)$$

LRAM

$$(20)(30) + (30)(10) + (40)(10) + 55(20) + 15(20)$$

3700 Gallons

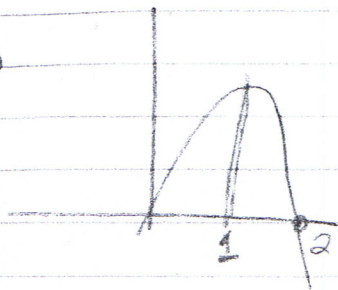
Yes Because the function is increasing on its domain and the rectangles would be enclosed

13. Omit

A, D

14. A

15



L RAM

R RAM

$$\begin{aligned}
 f(0) &= 1 \\
 f(1.25) &= .9375 \\
 f(1.5) &= .75 \\
 f(1.75) &= .4375 \\
 \hline
 & (3.125)(.25)
 \end{aligned}$$

$$\begin{aligned}
 f(1.25) &= .9375 \\
 f(1.50) &= .75 \\
 f(1.75) &= .4375 \\
 f(2.0) &= 0 \\
 \hline
 & (2.125)(.25)
 \end{aligned}$$

$$A = .78125$$

$$A = .53125$$

T RAM

$$\frac{.25}{2} [1 + 2(.9375) + 2(.75) + 2(.4375) + 0]$$

$$\frac{.25}{2} [5.25]$$

$$A = .65625$$

M RAM

$$.25 [ .98438 + .85938 + .60938 + .23438 ]$$

$$.67188$$