

### 3.3 Increasing/Decreasing Functions

\* What is the value of the derivative when a function is:

- a) Increasing  $f'(x) > 0$  positive
- b) Decreasing  $f'(x) < 0$  negative
- c) Constant  $f'(x) = 0$  zero

### \* First Derivative Test

Let  $c$  be a critical number of a function  $f$  that is continuous on an open interval containing  $c$ . If  $f$  is differentiable on the interval (except possibly  $c$ ), then  $f(c)$  can be classified as follows.

- 1)  $f'(x)$  pos  $\rightarrow$  neg, then rel max at  $(c, f(c))$
- 2)  $f'(x)$  neg  $\rightarrow$  pos, then rel min at  $(c, f(c))$
- 3)  $f'(x)$  pos on both sides of  $c$  or neg on both sides of  $c$ , then  $f(c)$  is neither a rel max nor min.