

Initial Value Problem 1:

Solve using 2 methods without a calculator.

1. $y' = 2 + \frac{1}{x^2}$ and $y(1) = 6$. Find $y(3)$.

Solve with a calculator.

3. $f'(x) = \cos(x^3)$ and $f(0) = 2$. Find $f(1)$.

4. $f'(x) = e^{-x^2}$ and $f(5) = 1$. Find $f(2)$.

Initial Value Problem 2:

Solve with a calculator.

5. A particle moving along the x -axis has position $x(t)$ at time t with the velocity of the particle $v(t) = 5 \sin(t^2)$. At time $t = 6$, the particle's position is $(4, 0)$. Find the position of the particle when $t = 7$.

6. Let $F(t)$ represent a bacteria population which is 4 million at time $t = 0$. After t hours, the population is growing at an instantaneous rate of 2^t million bacteria per hour. Find the total increase in the bacteria population during the first three hours, and find the population at $t = 3$ hours.

7. A particle moves along a line so that at any time $t \geq 0$ its velocity is given by $v(t) = \frac{t}{1+t^2}$.

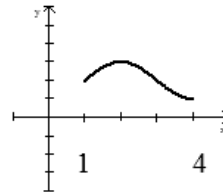
At time $t = 0$, the position of the particle is $s(0) = 5$. Determine the position of the particle at $t=3$.

Initial Value Problem 3 (with Graph):

Use the Fundamental Theorem of Calculus and the given graph.

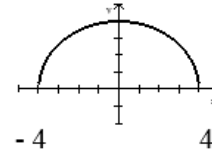
8. The graph of f' is shown on the right.

$$\int_1^4 f'(x) dx = 6.2 \text{ and } f(1) = 3. \text{ Find } f(4).$$



9. The graph of f' is the semicircle shown on the right.

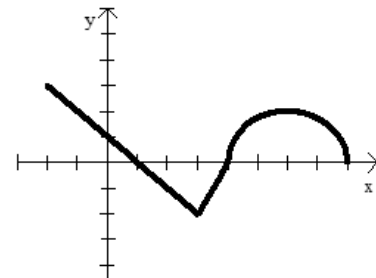
Find $f(-4)$ given that $f(4) = 7$.



10. The graph of f' , consisting of two line segments and a semicircle, is shown on the right.

Given that $f(-2) = 5$, find:

- (a) $f(1)$ (b) $f(4)$ (c) $f(8)$

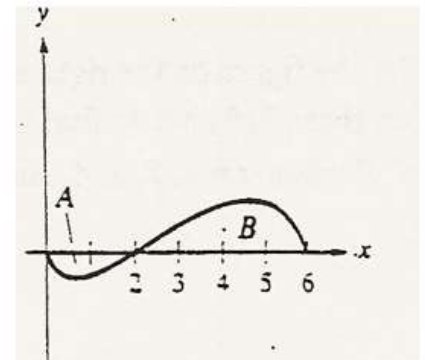


Initial Value Problem 4 (with Graph):

11. Region A has an area of 1.5, and $\int_0^6 f(x) dx = 3.5$. Find:

(a) $\int_2^6 f(x) dx$

(b) $\int_0^6 |f(x)| dx$

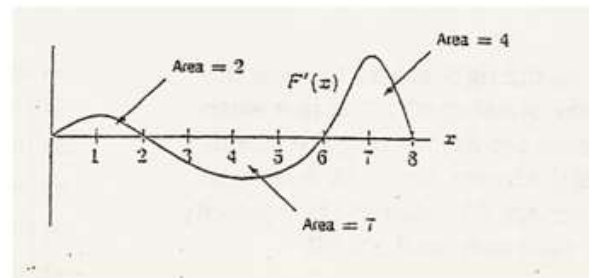


14. Given the figure on the right and the fact that $F(2) = 3$.

(a) Find $F(0)$, $F(6)$, and $F(8)$.

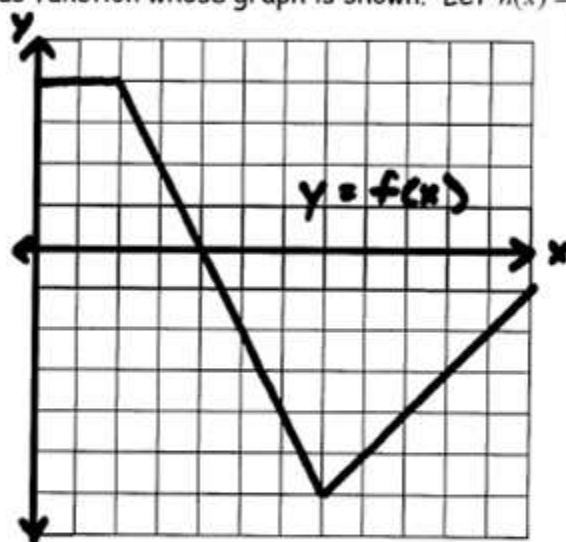
(b) Determine the intervals where the graph of F is increasing and decreasing. Justify your answer.

(c) Determine the intervals where the graph of F is concave up and concave down. Justify your answer.



FTC Applications FRQ 1:

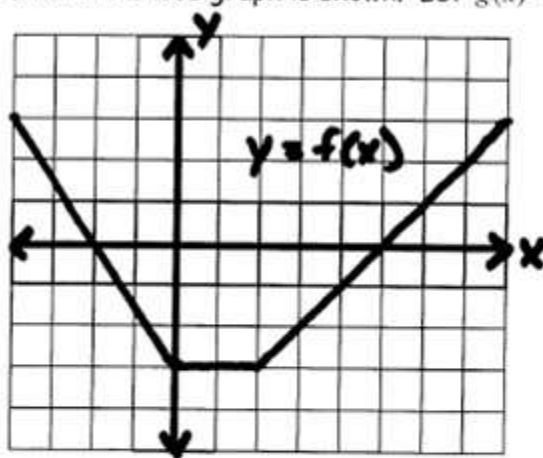
1. Let f be a continuous function whose graph is shown. Let $h(x) = \int_0^x f(t) dt$ for $0 \leq x \leq 12$.



- Find $h(3)$, $h'(3)$, and $h''(3)$.
- For what set of values of x is h decreasing?
- At what value of x does h attain its maximum?
- At what value of x does h attain its minimum. What is the minimum value?

FTC Applications FRQ 2:

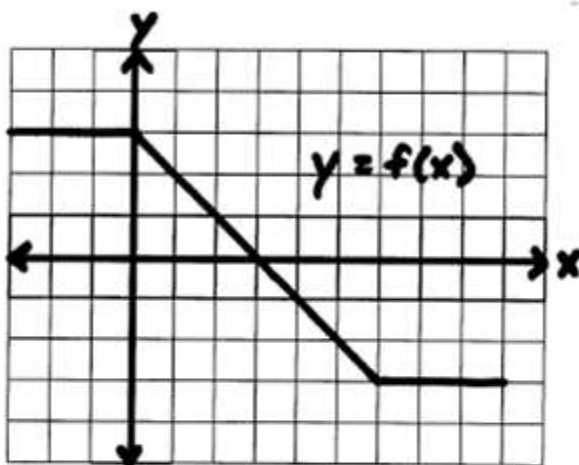
2. Let f be a continuous function whose graph is shown. Let $g(x) = \int_0^x f(t) dt$.



- Find the values of $g(-2)$, $g(2)$, and $g(8)$.
- Find the zeros of g .
- Find $g'(0)$, $g'(5)$, and $g'(8)$.
- Find $g''(3)$ and $g''(6)$.

FTC Applications FRQ 3:

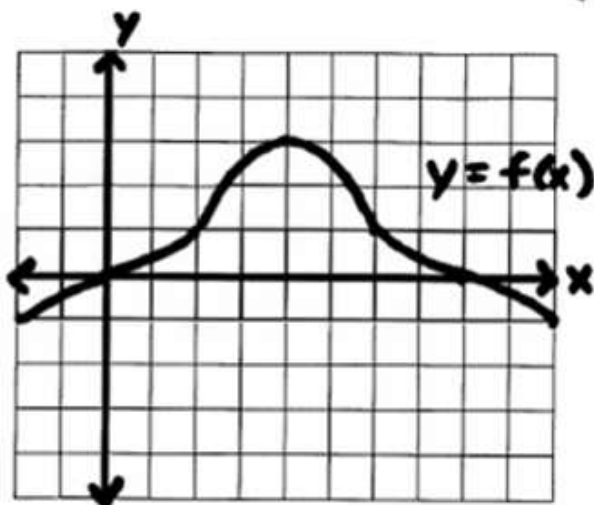
3. Let f be a continuous function whose graph is shown. Let $h(x) = \int_{-2}^x f(t) dt$ for $-3 \leq x \leq 9$.



- Find the zeros of h .
- On what interval(s) is h decreasing?
- What is $h(0)$?
- What is $h'(0)$?
- What is $h''(0)$?
- On what intervals is h concave down?

FTC Applications FRQ 4:

4. The graph of a differentiable function f on the closed interval $[-2, 10]$ is shown. The graph of f has a horizontal tangent line at $x = 4$. Let $g(x) = 5 + \int_4^x f(t) dt$ for $-2 \leq x \leq 10$.



- Find $g(4)$, $g'(4)$, and $g''(4)$.
- On what interval(s) is g decreasing. Justify your answer.
- On what interval(s) is the graph of g concave down? Justify your answer.
- At what x -value(s) does g have a point of inflection? Justify your answer.

Motion FRQ 1:

1. (Non-Calculator) The velocity of a moving particle on a coordinate line is given by $v(t) = t^2 + 3t - 10$ ft/min, where t is measured in minutes and $t \geq 0$.
- Find the displacement of the particle during the first 3 minutes.
 - Find when the particle's speed is decreasing. Justify.
 - Write, but do not evaluate, an integral expression to find the total distance traveled by the particle for the first 5 minutes.

Motion FRQ 2:

2. (Non-Calculator) Given the acceleration of the particle is $a(t) = -4$ ft/sec² and $v(0) = 12$ ft/sec during the interval $0 \leq t \leq 8$.
- Find the average velocity of the particle for the interval $0 \leq t \leq 8$.
 - Find when the instantaneous velocity of the particle is equal to the average velocity from part (a).
 - Find when the velocity is increasing.
 - Find the total distance traveled by the particle during the interval $0 \leq t \leq 8$.

Motion FRQ 3:

3. (Calculator) The velocity function of a moving particle is $v(t) = 3\cos(2t)$ in/hr for $0 \leq t \leq 2\pi$ hours.
- Determine when the particle is moving to the right. Justify.
 - Find the total distance traveled by the particle during the time interval $0 \leq t \leq 2\pi$ hours.
 - Given $x(0) = 5$, find $x(6)$.
 - Find when the particle is speeding up.

Motion FRQ 4:

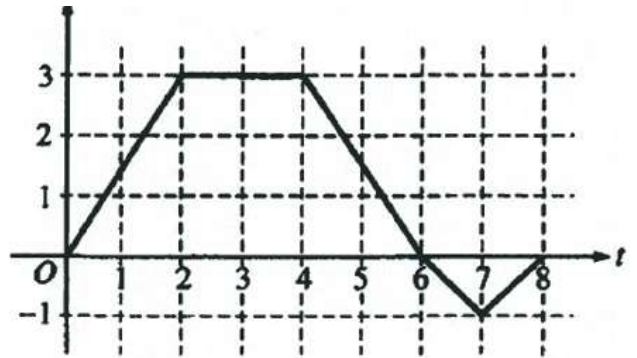
4. (Non-Calculator) A particle moves along the x -axis so that, at any time $t \geq 0$, its acceleration is given by $a(t) = 6t + 6$. At time $t = 0$, the velocity of the particle is -9 and its position is -27 .
- Find $v(t)$, the velocity of the particle at any time $t \geq 0$.
 - For what values of $t \geq 0$ is the particle moving to the right?
 - Find $x(t)$, the position of the particle at any time $t \geq 0$.

Motion MC 1 (Calculator Inactive):

A bug begins to crawl up a vertical wire at time $t = 0$. The velocity v of the bug at time t , $0 \leq t \leq 8$, is given by the function whose graph is shown above.

2. What is the total distance the bug traveled from $t = 0$ to $t = 8$?

- a. 14
- b. 13
- c. 11
- d. 8
- e. 6



5. A particle moves along the x -axis so that its acceleration at any time t is $a(t) = 2t - 7$. If the initial velocity of the particle is 6, at what time t during the interval $0 \leq t \leq 4$ is the particle farthest to the right?

- a. 0
- b. 1
- c. 2
- d. 3
- e. 4

Motion MC (Calculator Active):

8. At time $t \geq 0$, the acceleration of a particle moving on the x -axis is $a(t) = t + \sin t$. At $t = 0$, the velocity of the particle is -2 . For what value of t will the velocity of the particle be zero?

- a. 1.02
- b. 1.48
- c. 1.85
- d. 2.81
- e. 3.14

11. A particle moves along the x -axis so that at any time $t \geq 0$, its velocity is given by $v(t) = \cos(2 - t^2)$. The position of the particle is 3 at time $t = 0$. What is the position of the particle when its velocity is first equal to 0?

- a. 0.411
- b. 1.310
- c. 2.816
- d. 3,091
- e. 3.411