

* b) $f(x) = \cos x$ on $[0, 2\pi]$

① cont. on $[0, 2\pi]$ ✓

② dif. on $[0, 2\pi]$ ✓

③ $f(0) = f(2\pi)$
 $\cos 0 = \cos 2\pi$ ✓

RT \Downarrow

$$f'(x) = -\sin x = 0$$

$$\sin x = 0$$

$$x = 0, \pi, 2\pi, \dots$$

not in $(0, 2\pi)$

$$C = \pi$$

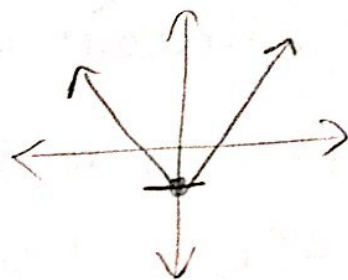
* c) $f(x) = |x| - 1$ on $[-1, 1]$

① cont on $[-1, 1]$ ✓

② dif on $[-1, 1]$ NO!

corner at $x=0$

RT \Downarrow



* Mean Value Theorem:

Let f be continuous on $[a, b]$ and differentiable on (a, b) .

Then there exists a $c \in (a, b)$ such that

$$\frac{\Delta y}{\Delta x}$$

$$\frac{f(b) - f(a)}{b - a} = f'(c)$$

↓
 endpoints slope
 (secant)

slope of
 tangent

↓
 slope @ a
 point