

c)  $g(x) = \csc x$  on  $[\frac{\pi}{6}, \frac{\pi}{3}]$

$$g'(x) = -\csc x \cot x = -\frac{1}{\sin x} \cdot \frac{\cos x}{\sin x} = \frac{-\cos x}{\sin^2 x}$$

$$-\cos x = 0$$

$$x = \frac{\pi}{2}, \frac{3\pi}{2}, \dots$$

$$\sin^2 x = 0$$

$$x = 0, \pi, \dots$$

NOT IN INTERVAL!

$x$	$g(x)$	
$\frac{\pi}{6}$	$\csc \frac{\pi}{6} = \frac{1}{\sin \frac{\pi}{6}} = 2$	Abs MAX: $(\frac{\pi}{6}, 2)$
$\frac{\pi}{3}$	$\csc \frac{\pi}{3} = \frac{1}{\sin \frac{\pi}{3}} = \frac{2}{\sqrt{3}} \approx 1.15$	Abs MIN: $(\frac{\pi}{3}, \frac{2}{\sqrt{3}})$

### \* Rolle's Theorem:

Let  $f$  be continuous on  $[a, b]$  and differentiable on  $(a, b)$ .

If  $f(a) = f(b)$ , there exists at least one number  $c \in (a, b)$  such that  $f'(c) = 0$ .

